

Humidity Profiling with a VHF Wind Profiler and GPS Measurements

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OUTLINE

- **Measurement principles and basic equations**
- **Implementation concerns**
- **Simulations using radiosondes**
- **The Puy de Dome framework**
- **Concluding remarks**

Measurement principles: the Basics

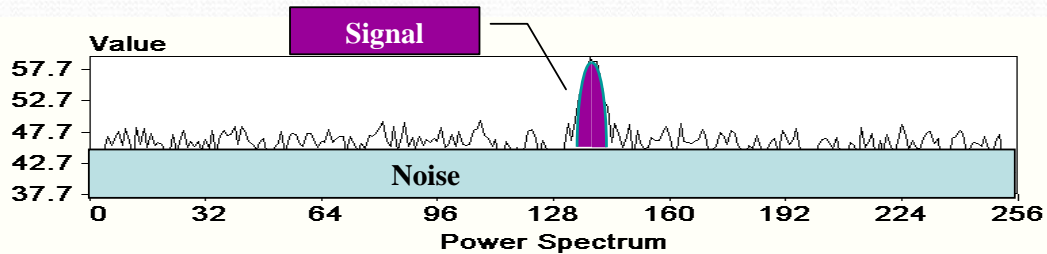
▪ Radar Measurements

SNR → Reflectivity

Spectral width → Turbulent dissipation rate

$$\eta = \alpha \cdot r^2 \frac{\text{Signal}}{\text{Noise}}$$

$$\varepsilon \approx 0,5N\sigma^2 \quad \text{or} \quad \varepsilon = f(\sigma)$$



▪ Temperature Profile -> N

- Radiometer, climatology ...

$$N^2 = g \cdot \frac{d \ln \theta}{dz} = \frac{g}{T} \cdot \left(\frac{dT}{dz} + \Gamma \right)$$

▪ At least 1 humidity reference

(point measurement or integrated)

- GPS, AMDAR, ...

Basic Equations (part 1) (Tsuda et al., 2001)

Refractive Index Gradient : M → q

$$M = -77,6 \times 10^{-6} \cdot \frac{P}{T} \left[\frac{N^2}{g} \cdot \left(1 + 15600 \frac{q}{T} \right) - \frac{7800}{T} \frac{dq}{dz} \right]$$

$$\frac{dq}{dz} - \left(\frac{2N^2}{g} \right) q = 1,652 \frac{T^2}{P} M + \frac{T}{7800} \frac{N^2}{g}$$

Where: $N^2 = g \cdot \frac{d \ln \theta}{dz} = \frac{g}{T} \cdot \left(\frac{dT}{dz} + \Gamma \right)$

$$q(z) = \theta^2 \left\{ \int_{z_0}^z \left[1,652 \frac{T^2}{P} M + \frac{1}{7800} \left(\frac{dT}{dz} + \Gamma \right) \right] \theta^{-2} dz + \frac{q_0}{\theta_0^2} \right\}$$

Radar Measurements → M

$$|M| = K L_0^{-2/3} \eta^{1/2}$$

(Gage and Balsley, 1980)

L_0 = External Scale (constant ?)

$$|M| = K' F^{1/2} N \varepsilon^{-1/3} \eta^{1/2}$$

(Tsuda et al., 2001)

F = Filling Factor (constant ?)

Signe of M ? (> 0 si $N^2 <$ threshold)

Basic Equations (part 2) (Stankov et al., 2003)

Potential Refractivity Gradient : $\phi \rightarrow q$

(Gossard et al. 1995)

$$\left. \begin{aligned} \frac{\partial \phi}{\partial \theta} &= -\frac{77,6 p_r}{\theta^2} \left(1 + 15,46 \frac{q}{\theta} \right) = -a_0 \\ \frac{\partial \phi}{\partial q} &= 77,6 p_r \frac{7,73}{\theta^2} = b_0 \end{aligned} \right\}$$

Estimated from
Standard Atmosphere

$$\phi = \frac{77,6 p_r}{\theta} \left(1 + \frac{7,73 q}{\theta} \right)$$

$$\frac{d\phi}{dz} = \frac{\partial \phi}{\partial \theta} \cdot \frac{d\theta}{dz} + \frac{\partial \phi}{\partial q} \cdot \frac{dq}{dz}$$

$$\frac{dq}{dz} = \left[\frac{d\phi}{dz} + a_0 \frac{d\theta}{dz} \right] \cdot b_0^{-1}$$

$$q(z) = \int q(z_0) + [\phi(z) - \phi(z_0) + a_0(\theta(z) - \theta(z_0))] \cdot b_0^{-1}$$

Radar Measurement $\rightarrow \phi$

(Gossard et al., 1982)

$$\left(\frac{d\phi}{dz} \right)^2 = \frac{C_\phi^2}{C_w^2} \left(\frac{L_w}{L_\phi} \right)^{4/3} S^2$$

Structure Parameters

External Scale

Horizontal Wind Shear: S

$$C_\phi^2 = \frac{\eta}{0.38} \lambda^{1/3}$$

$$C_w^2 \approx 2.80 \epsilon^{2/3}$$

$$L_w / L_\phi \approx 2 \leftrightarrow 6$$

Potential Refractivity

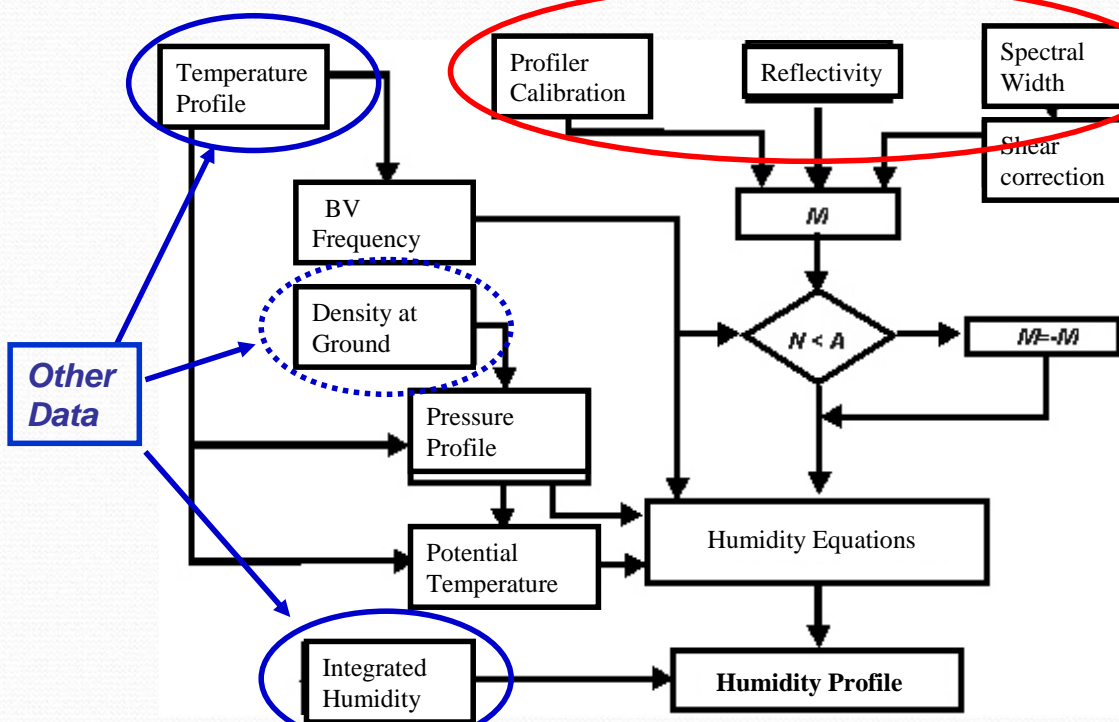
Vertical Velocity

L_w : for Vertical Velocity

L_ϕ : for Potential Refractivity

Practical Implementation Flow Chart

Radar



Practical Implementation: Example

q(z) Equation

$$q(z) = \theta^2 \left\{ \int_{z_0}^z \left[1,652 \frac{T^2}{P} M + \frac{1}{7800} \left(\frac{dT}{dz} + \Gamma \right) \right] \theta^{-2} dz + \frac{q_0}{\theta_0^2} \right\}$$

$$q(z) = 1,652 \theta^2 \int_{z_0}^z \frac{T^2 M}{P \theta^2} dz + \frac{\theta^2}{7800 g} \int_{z_0}^z \frac{T N^2}{\theta^2} dz + \theta^2 \frac{q_0}{\theta_0^2}$$

Radar :

$$M_{atm} = K M_{radar} = K M$$

$$q(z) = K a_0(z) + b_0(z) + c_0(z) q_0$$

+ Integrated form : $qt = K A_0 + B_0 + C_0 q_0$

2 unknowns: K et $q_0 \rightarrow$ 2 references needed

If qt and $q(z_i)$ known:

$$K = \frac{[q(z_i) - b_0(z_i)] \cdot C_0 - [qt - B_0] \cdot c_0(z_i)}{a_0(z_i) \cdot C_0 - A_0 \cdot c_0(z_i)}$$

$$q_0 = \frac{-[q(z_i) - b_0(z_i)] \cdot A_0 + [qt - B_0] \cdot a_0(z_i)}{a_0(z_i) \cdot C_0 - A_0 \cdot c_0(z_i)}$$

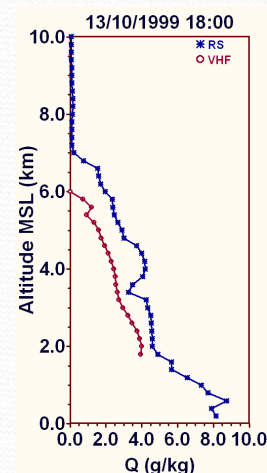
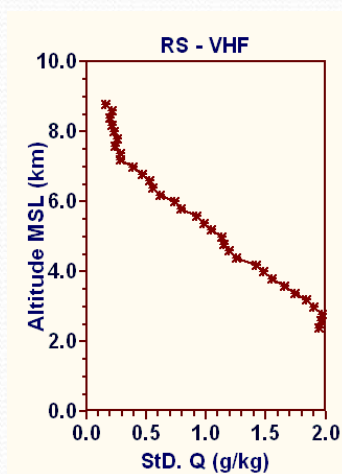
If $q(z_i)$ and $q(z_j)$ known:

$$K = \frac{[q(z_i) - b_0(z_i)] \cdot c_0(z_j) - [q(z_j) - b_0(z_j)] \cdot c_0(z_i)}{a_0(z_i) \cdot c_0(z_j) - a_0(z_j) \cdot c_0(z_i)}$$

$$q_0 = \frac{-[q(z_i) - b_0(z_i)] \cdot a_0(z_j) + [q(z_j) - b_0(z_j)] \cdot a_0(z_i)}{a_0(z_i) \cdot c_0(z_j) - a_0(z_j) \cdot c_0(z_i)}$$

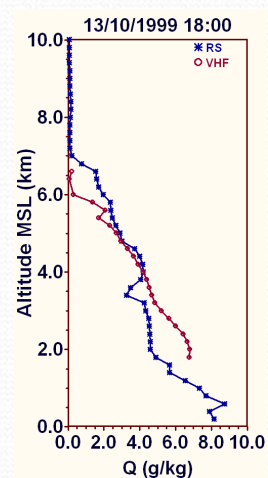
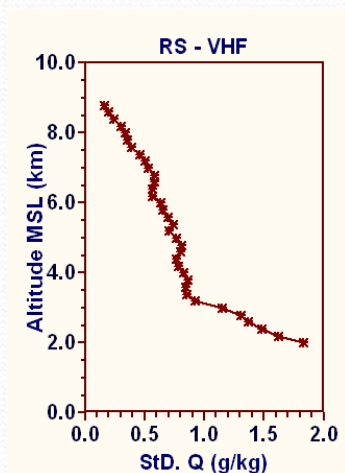
Simulations using RS (MAP 99)

1 reference value:
- $Q \approx 0$ at 9 km height



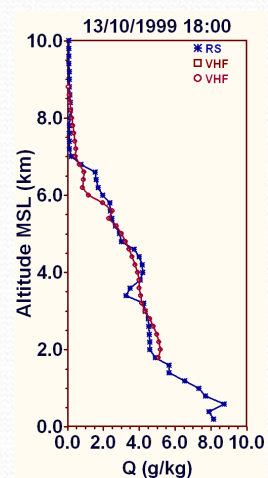
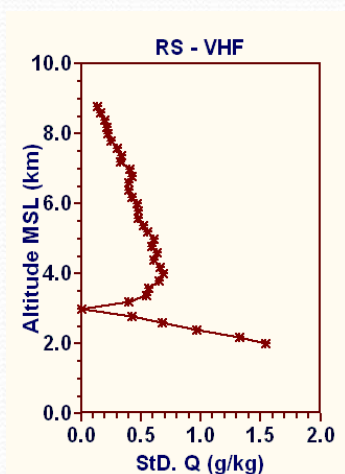
Simulations using RS (MAP 99)

- 2 reference values:
- $Q \approx 0$ at 9 km height
 - + total Q



Simulations using RS (MAP 99)

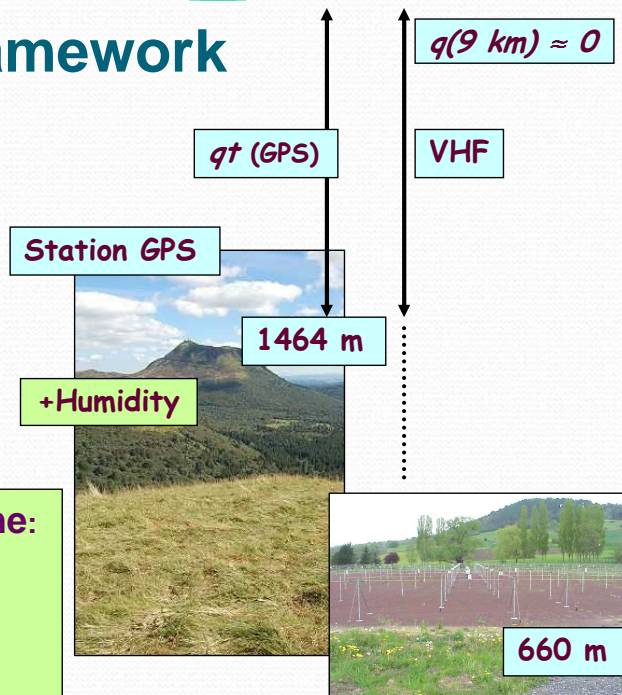
- 3 reference values:
- $Q \approx 0$ at 9 km height
 - + total Q
 - + Q at the base of the radar range (3 km in our example)



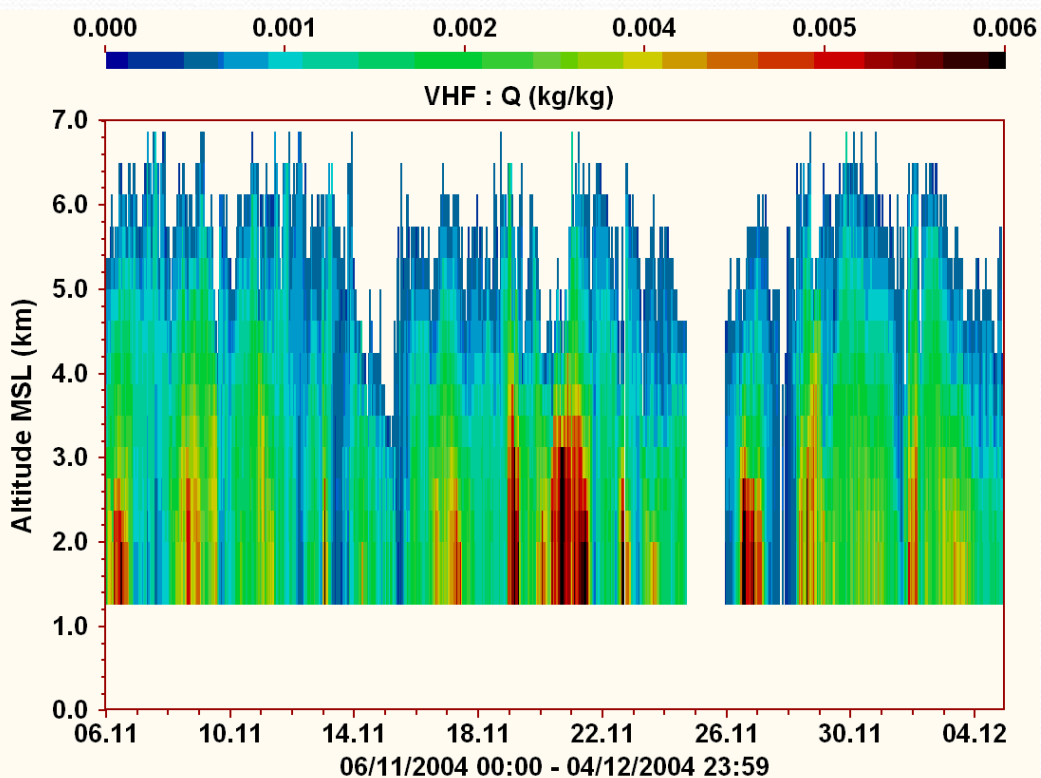
The puy de Dôme Framework

- VHF Profiler At Ompe
 - ⇔ Hypothesis $q(9 \text{ km}) \approx 0$
- Temperature Profile (Climatology)
- Profiler first gate and GPS station at puy de Dôme
 - ⇔ $qt = qt(\text{GPS})$
- → Humidity Profile

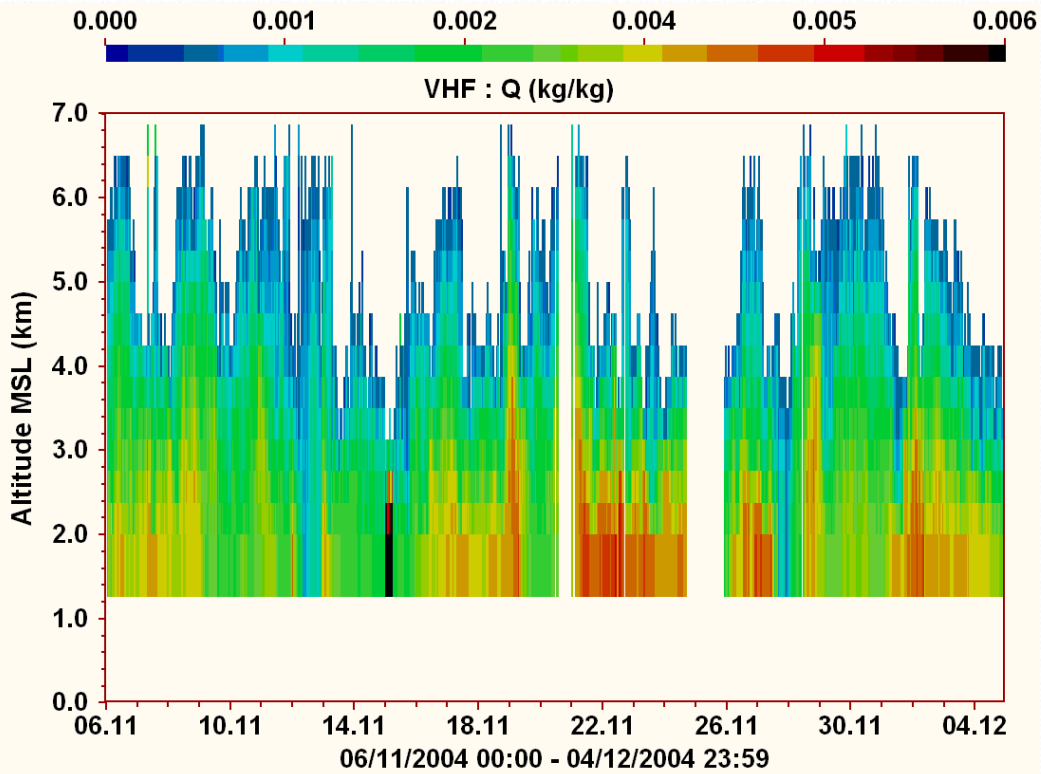
- + Humidity sensor at puy de Dôme:
 - Comparison possible between:
 - $(qt - q_{zi})$ and $(q_{zi} - q_{zi})$
 - Control of hypothesis coherency
 - Possibility to use
 - 3 equations with 3 unknowns: qt , $q(z_i)$ and $q(z_j)$
 - Allowing either
 - $L_0(z)$ (Gossard, Tatarskii)
 - $F(z)$ (Tsuda)



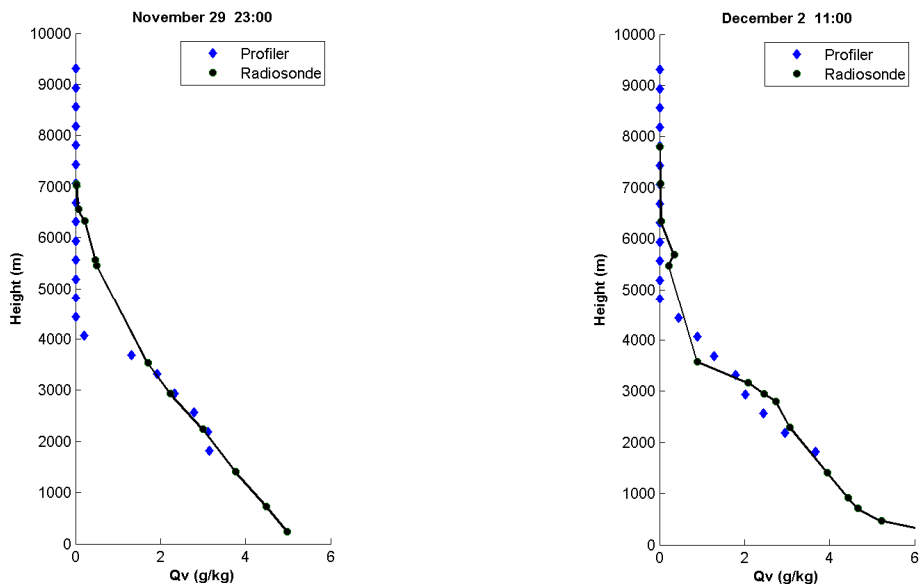
First Results: 6 Nov – 04 Dec 2004 -- (qt , q_{zi})



First Results: 6 Nov – 04 Dec 2004 -- (q_t , q_{zi} , q_{zj})



RS Comparisons (Lyon 160 km to East)

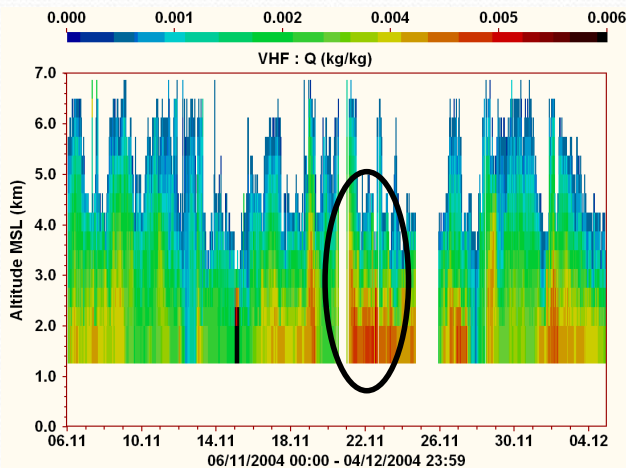
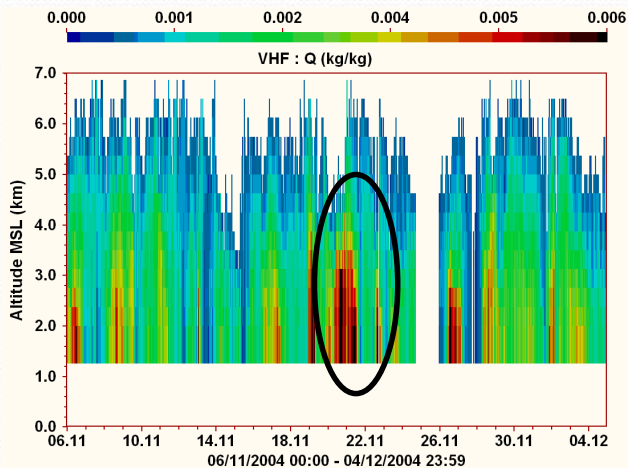


Using (q_t , q_{zi} , q_{zj}) results

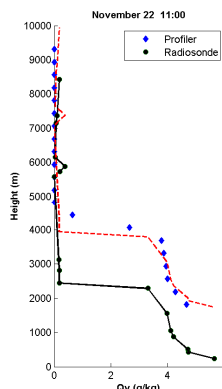
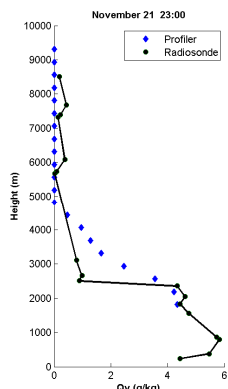
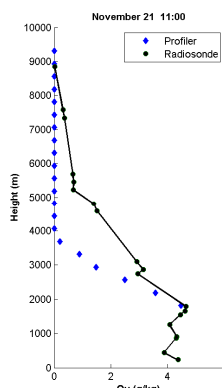
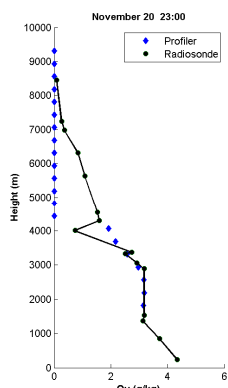
Some discrepancies between results !

With (qt, qzi)

With (qt, qzi, qzj)



RS Comparisons with (qt, qzi, qzj)



Conclusions

- The Puy de Dôme geographical configuration is optimum to test the synergy between :

- VHF profiler and GPS (qt)
- VHF profiler, GPS (qt) and In situ humidity sensor ($q_{Puy\ Dome}$)

in order to retrieve the humidity profile

- Preliminary results are encouraging:

- 3 parameter retrieval seems to improve restitution of humidity profile
- BUT... detailed testing and statistical comparison between different approaches still underway,
- ... need to understand differences with RS

- Future developments include:

- Comparison of humidity profiles retrieved with local Raman Lidar
- Measured temperature profile VS climatology based
- Real time application to get model analysis monitoring feedback, for future assimilation
- Increased altitude coverage towards BL with UHF profiler and local GPS network

Thank You for your Attention...

